

Solution

- a) The rule for `letrec` is like the rule for `let`, but we also add x to Γ when checking t_1 .

$$\frac{\Gamma[x: \sigma_1] \vdash t_1: \sigma_1 \quad \Gamma[x: \sigma_1] \vdash t_2: \sigma_2}{\Gamma \vdash (\mathbf{letrec} \ x = t_1 \ \mathbf{in} \ t_2): \sigma_2} \text{LETREC}$$

Alternatively, we can combine this rule with the \forall -intro typing rule:

$$\frac{\begin{array}{c} \{\alpha_1 \dots \alpha_n\} = FV(\tau) \setminus FV(\Gamma) \\ \Gamma[x: \forall \alpha_1 \dots \alpha_n. \tau] \vdash t_1: \tau \quad \Gamma[x: \forall \alpha_1 \dots \alpha_n. \tau] \vdash t_2: \tau_2 \end{array}}{\Gamma \vdash \mathbf{letrec} \ x = t_1 \ \mathbf{in} \ t_2: \tau_2} \text{LETREC}'$$

- b) The interesting property of this new typing rule is that we cannot know which $\alpha_1 \dots \alpha_n$ we need to generalize τ over before we have inferred τ (the type of t_1). Thus, typical compilers will only allow x to be used monomorphically in t_1 . Alternatively, the user can explicitly specify a type schema for x , so that it can be used polymorphically.

Exercise 3 (Type Inference in Haskell (2))

Extend the implementation of the type inference algorithm from the last exercise with `let` and `letrec` constructs.

You can find a template [here](#).

Solution

See [type_inference_let_sol.hs](#).

$$\frac{\frac{\frac{\vdots}{\Gamma \vdash t_1 : \tau}}{\Gamma \vdash t_1 : \forall \alpha_n. \tau} \forall\text{Intro}}{\Gamma \vdash t_1 : \forall \alpha_1, \dots, \alpha_n. \tau} \forall\text{Intro}$$